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## **PSEUDO-OFFSET MIGRATION:**

### BACKGROUND OF THE INVENTION:

This invention relates to the field of seismic data acquisition and processing.

Converted-wave (C-wave) processing is more difficult than pure-mode processing. Those of the ordinary skill in the art will recognize that converted waves result from compressional waves (P-waves), which come into contact with a reflecting surface and incite a shear wave (S-wave). The opposite is also true. That is, an S-wave may also incite a P-wave. Because P-waves and S-waves have different characteristics, converted wave processing, which requires a set of characteristics for the down-going wave and a different set of characteristics for the up-going wave, is much more complicated than processing only a single set of characteristics for only P-wave data or S-wave data.

For example, accurate migration is critically dependent on both P-wave and S-wave velocities. Furthermore, conventional prestack time migration techniques, such as the industry standard of Kirchhoff migration, are normally based on the double-square root travel time equation. These methods assume a straight ray from the source to the scatter point and from the scatter point to the receiver. Other current Kirchhoff prestack time migration techniques are often implemented with a travel time approximation (Li et al., 2001). The straight ray assumption and the travel time approximation thus, limit the ability to produce an accurate subsurface image without a correction for ray bending and

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travel time errors. For multi-layered v(z) media or vertical transversely isotropic (VTI) media, more sophisticated travel time equations are needed.

Even further, another current prestack migration is equivalent-offset migration. Equivalent-offset migration (EOM) is a prestack time migration method proposed by Bancroft et al. (1998). Equivalent offset migration claims to be computationally efficient and weakly velocity-dependent. However, in C-wave processing, equivalent offset migration (Wang et al, 1996) depends on the initial velocity even for a single constant-velocity flat layer. Thus, EOM is poor for C-wave velocity analysis.

Finally, many current ocean bottom cable (OBC) techniques require waveequation datumming. Wave equation datumming adds additional processing steps, increases cost, and causes irregular geometry effects on 3-D OBC data processing.

Thus, there is a long felt need for migration techniques which address one or any of the above issues.

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#### SUMMARY OF THE INVENTION:

In one example embodiment of the present invention, a method is provided for migrating an input seismic data point having an input source location, an input receiver location, and an image location associated therewith. The method comprises determining a pseudo-offset, and mapping the seismic data point to the image location based at least in part on the pseudo-offset.

In a further example embodiment of the present invention, a method is provided for migration of a seismic data point having an input source location, an input receiver location, and a scatter point associated therewith. The method comprises determining a projected source location and determining a projected receiver location. The method further comprises mapping the seismic data point from the input travel time to a projected travel time. The method also comprises determining a pseudo-offset based at least in part on the projected travel time, and mapping the data point to the pseudo-offset.

In an even further example embodiment of the present invention, a method of performing velocity analysis on a seismic gather is provided. The method comprises computing a moveout travel time based on an initial model and computing an intermediate travel time. The method further comprises mapping the gather from the moveout travel time to the intermediate travel time, and scanning for velocities based on the intermediate travel time.

In an even further embodiment, a system is provided for migrating an input seismic data point having an input source location and an input receiver location, a scatter point, and an image location associated therewith. The system comprises means for

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determining a pseudo-offset, and means for mapping the seismic data point to the image location based at least in part on the pseudo-offset.

In an even further embodiment, a system is provided for migration of a seismic data point having an input source location, an input receiver location, and a scatter point associated therewith. The system comprises means for determining a projected source location, means for determining a projected receiver location, means for mapping the seismic data point from an input travel time to a projected travel time, means for determining a pseudo-offset based on the projected travel time, and means for mapping the data point to the pseudo-offset.

In an even further embodiment, a system for performing velocity analysis on a seismic gather is provided. The system comprises means for computing a moveout travel time based on an initial model, means for computing an intermediate travel time, means for mapping the gather from the moveout travel time to the intermediate travel time, and means for scanning for velocities based on the intermediate travel time.

In an even further embodiment, a seismic data point is provided. The seismic data point is produced by the process of migration comprising determining a pseudo-offset, and mapping the seismic data point to the image location based at least in part on the pseudo-offset.

In an even further embodiment, a seismic data point is provided. The seismic data point is produced by a method of migration comprising determining a projected source location, determining a projected receiver location, mapping the seismic data point from

the input travel time to a projected travel time, determining a pseudo-offset based on the projected travel time, and mapping the data point to the pseudo-offset.

# **BRIEF DESCRIPTION OF THE FIGURES:**

FIGURE 1 is a diagram outlining an example embodiment of the present invention.

FIGURE 2 is a schematic diagram demonstrating features of an example embodiment of the present invention.

FIGURE 3 is a diagram outlining an example embodiment of the present invention.

FIGURE 4 is a schematic diagram demonstrating features of an example embodiment of the present invention.

FIGURE 5 is a diagram outlining an example embodiment of the present invention.

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# DETAILED DESCRIPTION OF EXAMPLE EMBODIMENTS OF THE INVENTION:

Those of ordinary skill in the art will appreciate that for the purpose of teaching the broad aspect of the present invention, example embodiments of the invention are described in detail.

As illustrated by reading Figures 1 and 2 in conjunction, in one example embodiment of the present invention, a method of migrating seismic data is provided. In alternate embodiments the content and acquisition situation of the seismic data to be migrated is land data, dual sensor data, streamer data, VSP data, vertical cable data, or any other data from any other acquisition situation that will occur to those of ordinary skill in the art. In a further embodiment, the seismic data comprises an input seismic data point having an input source location S and an input receiver location R. Those of ordinary skill in the art will recognize that such information is often available on the trace headers or geometry database. The method comprises determining (110) a pseudo-offset x and mapping (120) the seismic data point to the image location I based at least in part on the pseudo-offset x. In an even further embodiment, the method further comprises determining a pseudo-source S\* and a pseudo-receiver R\*. In still a further embodiment, the pseudo-source S\* and the pseudo-receiver R\* are not collocated. In an even further embodiment, the pseudo-offset x comprises a distance between the pseudo-source  $S^*$  and the image location I plus a distance between the pseudo-receiver R\* and the image In still an even further embodiment, the method further comprises location I.

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determining a pseudo ray parameter p. In an even further embodiment, determining a pseudo ray parameter p further comprises determining a pseudo ray parameter p which is constant from the pseudo-source  $S^*$  to the scatter point D and from the scatter point D to the pseudo-receiver  $R^*$ . In still a further embodiment, determining a pseudo-offset x further comprises determining a travel time associated with the input source location S and the input receiver location R and the scatter point D. In an even further embodiment, determining a pseudo-offset x further comprises determining a pseudo travel time from the pseudo-source  $S^*$  to the pseudo-receiver  $R^*$  via the scatter point D. In an even further embodiment, the pseudo travel time and the actual travel time from the input source location S to the input receiver location S are essentially equivalent.

In a further example embodiment of the present invention, a method of migrating seismic data is developed for multi-layered v(z) isotropic media. To demonstrate this we begin with the basic Kirchhoff integral for C-wave prestack time migration. The Kirchhoff integral is formulated as the following summation,

$$output(t_{C0}) = \sum_{aperture} amplitude [filter * input(t)], \tag{1}$$

where t is the input travel time which is the sum of the P-wave travel time  $t_P$  from a source S to a scatter point D and the S-wave travel time  $t_S$  from the scatter point D to a receiver R as illustrated in Figure 2. The travel time is,

$$t = t_{\mathbf{P}} + t_{\mathbf{S}}. \tag{2}$$

 $t_{\rm C0}$  is the C-wave vertical travel time which is the sum of the P-wave vertical travel time  $t_{\rm P0}$  and the S-wave vertical travel time  $t_{\rm S0}$ ,

$$t_{\rm C0} = t_{\rm P0} + t_{\rm S0} \,. \tag{3}$$

In one embodiment, for the v(z) media,  $t_P$  is computed from the following equation (Slotnick 1959),

$$t_{\rm P}(p_{\rm P}) = \int_0^{t_{\rm P0}} \frac{d\tau_{\rm P}}{\sqrt{1 - p_{\rm P}^2 v_{\rm P}^2(\tau_{\rm P})}},\tag{4}$$

where  $v_P(\tau_P)$  is the P-wave interval velocity, and  $p_P$  is a ray parameter from the source S to the scatter point D, which is solved from the following equation,

$$\int_{0}^{t_{P0}} \frac{p_{P} v_{P}^{2}(\tau_{P}) d\tau_{P}}{\sqrt{1 - p_{P}^{2} v_{P}^{2}(\tau_{P})}} = h_{P},$$
(5)

where  $h_P$  is the horizontal distance between the source S and the scatter point D. Similarly, in a further embodiment,  $t_S$  is computed from the following equation,

$$t_{\rm S}(p_{\rm S}) = \int_{0}^{t_{\rm S0}} \frac{d\tau_{\rm S}}{\sqrt{1 - p_{\rm S}^2 v_{\rm S}^2(\tau_{\rm S})}},\tag{6}$$

where  $v_S(\tau_S)$  is the S-wave interval velocity, and  $p_S$  is a ray parameter from the scatter point D to the receiver R, which is solved from the following equation,

$$\int_{0}^{t_{S0}} \frac{p_{S} v_{S}^{2}(\tau_{S}) d\tau_{S}}{\sqrt{1 - p_{S}^{2} v_{S}^{2}(\tau_{S})}} = h_{S},$$
(7)

where  $h_S$  is the horizontal distance between the scatter point D and the receiver R. To replace  $t_{P0}$  and  $t_{S0}$  with  $t_{C0}$  in equations above, let

$$\tau = \tau_{\mathbf{P}} + \tau_{\mathbf{S}},\tag{8}$$

and define the interval vertical travel time ratio as

$$\gamma_0(\tau) = d\tau_{\rm S}/d\tau_{\rm P} \ . \tag{9}$$

For the isotropic medium,  $y_0(\tau)$  is equal to the interval velocity ratio, that is

$$v_{\rm P}(\tau_{\rm P})/v_{\rm S}(\tau_{\rm S}) = \gamma_0(\tau). \tag{10}$$

In another example embodiment, we then use the C-wave interval velocity  $v_C(\tau)$  defined by Thomsen (1999),

$$v_{\rm C}^2(\tau) = \frac{v_{\rm P}^2(\tau_{\rm P})d\tau_{\rm P} + v_{\rm S}^2(\tau_{\rm S})d\tau_{\rm S}}{d\tau},\tag{11}$$

to replace velocities  $v_P(\tau_P)$  and  $v_S(\tau_S)$ . By substituting  $t_{P0}$ ,  $t_{S0}$ ,  $v_P$ , and  $v_S$  with  $t_{C0}$ ,  $v_C$ , and  $v_S$  in the travel time equations (4) - (7),  $t_P$  and  $t_S$  is computed using the following equations,

$$t_{\rm P}(p_{\rm P}) = \int_{0}^{t_{\rm C0}} \frac{\frac{1}{1 + \gamma_0(\tau)} d\tau}{\sqrt{1 - \gamma_0(\tau) p_{\rm P}^2 v_{\rm C}^2(\tau)}},$$
 (12)

$$\int_{0}^{t_{C_0}} \frac{\gamma_0(\tau)}{1 + \gamma_0(\tau)} p_P v_C^2(\tau) d\tau = h_P,$$
(13)

$$t_{\rm S}(p_{\rm S}) = \int_{0}^{t_{\rm C0}} \frac{\frac{\gamma_0(\tau)}{1 + \gamma_0(\tau)} d\tau}{\sqrt{1 - \frac{1}{\gamma_0(\tau)} p_{\rm S}^2 v_{\rm C}^2(\tau)}},$$
(14)

$$\int_{0}^{t_{C0}} \frac{\frac{1}{1 + \gamma_{0}(\tau)} p_{S} v_{C}^{2}(\tau) d\tau}{\sqrt{1 - \frac{1}{\gamma_{0}(\tau)} p_{S}^{2} v_{C}^{2}(\tau)}} = h_{S}.$$
 (15)

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In an even further embodiment, for the isotropic media, we only need to know  $t_{CO}$ ,  $\nu_{C}$ , and  $\gamma_{C}$  to compute  $t_{P}$  and  $t_{S}$ . Unlike conventional techniques, no effective velocity ratio  $\gamma_{eff}$  (Thomsen, 1999) is required. In alternate embodiments, the interval vertical travel time ratio  $\gamma_{C}$  is determined directly from the travel time ratio of corresponding C-wave and P-wave events such as on stacks or extrapolated from oblique times on prestack gathers.

In an even further embodiment, instead of performing the Kirchhoff summation directly as is done in conventional migration, we divide the Kirchhoff summation into two steps. The first step is to map each input sample to a new geometry, such that, two conditions are met. The first condition is that the travel time from the new source  $S^*$  (called the pseudo-source) to the new receiver  $R^*$  (called the pseudo-receiver) is essentially the same as the travel time computed from the input geometry of the input source location S and the input receiver location S, as illustrated in Figure 2. The second condition is the ray parameter from the new pseudo-source  $S^*$  to the scatter point D is essentially the same as the ray parameter from the scatter point D to the new pseudo-receiver  $S^*$ . We call the new ray parameter the pseudo ray parameter  $S^*$ . In a further embodiment, the pseudo ray parameter  $S^*$  is computed from the following equations.

$$t = t_{\rm P}(p_{\rm P}) + t_{\rm S}(p_{\rm S}),$$
 (16)

$$t^*(p) = t, \tag{17}$$

$$t^*(p) = t_P(p) + t_S(p),$$
 (18)

where  $t^*$  is the new travel time from the pseudo-source to the pseudo-receiver and is called the pseudo travel time. As illustrated in Figure 2, the distance between the pseudo-

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source  $S^*$  and the image location I plus the distance between the pseudo-receiver  $R^*$  and the image location I is called the pseudo-offset x. In an even further embodiment, with the estimated pseudo ray parameter p, the pseudo-offset x is computed as follows

$$x = \int_{0}^{t_{C0}} \left[ \frac{\gamma_0(\tau)}{\sqrt{1 - \gamma_0(\tau) p^2 v_C^2(\tau)}} + \frac{1}{\sqrt{1 - \frac{1}{\gamma_0(\tau)} p^2 v_C^2(\tau)}} \right] \frac{p v_C^2(\tau) d\tau}{1 + \gamma_0(\tau)}.$$
 (19)

For a given scatter point D, the input samples inside the migration aperture are accumulated to different pseudo-offsets x based on the equations (16) - (19). Thus, a common-scatter point gather or POM gather is created. We call the first step migration mapping. The second step of this migration scheme is to perform moveout correction based on equation (18) and stack the POM gather along the pseudo travel time. We call the second step migration stacking.

In an even further embodiment, the pseudo-offset migration method is employed in the ocean-bottom cable (OBC) acquisition situation. The OBC option assumes the elevation difference between shots and receivers and performs the migration without wave-equation datuming (Berryhill, 1979). For the OBC data migration, we assume the velocity function is referenced at the sea level where shots are normally located, so  $t_P$  is still computed based on equations (12) – (13). However, in an even further embodiment of the present invention, the computation for  $t_S$  is redefined. Assuming  $d_r$  is the receiver depth,  $\nu_w$  is the P-wave replacement velocity or the water velocity, and  $\gamma_w$  is a replacement value for the shallow  $\gamma_0$ , equations (14) and (15) are replaced by

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$$t_{\rm S}(p_{\rm S}) = \int_{0}^{t_{\rm C0}} \frac{\frac{\gamma_0(\tau)}{1 + \gamma_0(\tau)} d\tau}{\sqrt{1 - \frac{1}{\gamma_0(\tau)} p_{\rm S}^2 v_{\rm C}^2(\tau)}} - \frac{\gamma_w d_r}{v_w \sqrt{1 - \frac{p_{\rm S}^2 v_w^2}{\gamma_w^2}}}.$$
 (20)

$$\int_{0}^{t_{C0}} \frac{\frac{1}{1+\gamma_{0}(\tau)} p_{S} v_{C}^{2}(\tau) d\tau}{\sqrt{1-\frac{1}{\gamma_{0}(\tau)} p_{S}^{2} v_{C}^{2}(\tau)}} - \frac{p_{S} v_{w} d_{r}}{\gamma_{w} \sqrt{1-\frac{p_{S}^{2} v_{w}^{2}}{\gamma_{w}^{2}}}} = h_{S}.$$
(21)

Those of ordinary skill in the art will recognize that in alternate embodiments, pseudo-offset migration is still performed based on equations (16) - (18). In an even further embodiment, the pseudo-offset migration method is employed for OBC, vertical cable, VSP, or land data migration or any other acquisition situation that will occur to those of ordinary skill in the art.

Turning now to Figures 3 and 4 in conjunction, a further example embodiment of the present invention is presented. A method of migrating a seismic data point having an input source location, an input receiver location, and a scatter point associated therewith is provided. The method comprises determining (310) a projected source location S', determining (320) a projected receiver location R', mapping (330) the input seismic data point from the input travel time t to a projected travel time t, determining (340) a pseudo-offset x based on the projected travel time t, and mapping (350) the input sample to the pseudo-offset. In alternate embodiments, the projected source location S' and/or the projected receiver location R' are unmoved, or essentially equivalent, to the input source location S and the input receiver location R. In even further alternate embodiments, the projected source location R' are

projected along the raypath of the input source location S to the scatter point D to the input receiver location R. In a further embodiment, the projected source location S' is controlled by the ray parameter  $p_P$  which is solved from equation,

$$\int_{0}^{t_{C0}} \frac{\frac{\gamma_{0}(\tau)}{1 + \gamma_{0}(\tau)} p_{P} v_{C}^{2}(\tau) d\tau}{\sqrt{1 - \gamma_{0}(\tau) p_{P}^{2} v_{C}^{2}(\tau)}} - \frac{p_{P} v_{w} d_{s}}{\sqrt{1 - p_{P}^{2} v_{w}^{2}}} = h_{P},$$
(22)

where the C-wave interval velocity  $v_C(\tau)$  is referenced at a datum (401) and  $d_s$  is the distance from the source location S to the datum (401). In an even further embodiment, the projected receiver location R' is controlled by the ray parameter  $p_S$  which is solved from equation (21) where  $d_r$  is the distance from the receiver location R to the datum (401). In yet a further embodiment, with  $p_P$  and  $p_S$ , the input travel time are computed as

$$10 t = \int_{0}^{t_{C0}} \frac{\frac{1}{1 + \gamma_0(\tau)} d\tau}{\sqrt{1 - \gamma_0(\tau) p_P^2 v_C^2(\tau)}} - \frac{d_s}{v_w \sqrt{1 - p_P^2 v_w^2}} + \int_{0}^{t_{C0}} \frac{\frac{\gamma_0(\tau)}{1 + \gamma_0(\tau)} d\tau}{\sqrt{1 - \frac{1}{\gamma_0(\tau)} p_S^2 v_C^2(\tau)}} - \frac{\gamma_w d_r}{v_w \sqrt{1 - \frac{p_S^2 v_w^2}{\gamma_w^2}}}. (23)$$

In still a further embodiment, the projected travel time from S' to D and from D to R' is determined by

$$t' = \int_{0}^{t_{C0}} \frac{\frac{1}{1 + \gamma_{0}(\tau)} d\tau}{\sqrt{1 - \gamma_{0}(\tau) p_{P}^{2} v_{C}^{2}(\tau)}} + \int_{0}^{t_{C0}} \frac{\frac{\gamma_{0}(\tau)}{1 + \gamma_{0}(\tau)} d\tau}{\sqrt{1 - \frac{1}{\gamma_{0}(\tau)} p_{S}^{2} v_{C}^{2}(\tau)}}.$$
 (24)

The input sample point is mapped from t to t'. In an even further embodiment, the pseudo ray parameter p is determined by

$$t^*(p) = t'. (25)$$

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In yet another example embodiment, the pseudo-offset is computed with equation (19).

Those of ordinary skill in the art will recognize that the amplitude term in equation (1) contains both the spherical divergence recovery and the obliquity factor (Yilmaz, 1987). The filter term in equation (1) represents several functions in alternate embodiments. The first function is that of a band-pass filter. The second function is that it performs statics correction. The third function is that it operates as a derivative filter, which performs the first-order derivative filtering for 3-D data and the half-order derivative filtering for 2-D data (Yilmaz, 1987). The last function is that it operates as an antialiasing filter. The antialiasing filter is designed for each input/output trace pair. To apply the antialiasing for each input/output pair, even the 3-point triangle filter (Lumley et al., 1994) will increase the migration runtime significantly. In alternate embodiments, to cut the cost and still reject the aliasing noise, an amplitude weighting technique is developed. The weighting coefficients are defined as follows,

$$w = \frac{V_{\rm C2}^2 t \Delta t}{4r \Delta r},\tag{26}$$

where  $\Delta t$  is the sample interval, r is the migration radius which is the distance from the conversion point (C-wave) or midpoint (P-wave) to the scatter point,  $\Delta r$  is the sample interval of the migration radius, and  $V_{\rm C2}$  is the C-wave short-spread moveout velocity.

In another example embodiment of the present invention, a method of migrating seismic data is developed for vertical transversely isotropic (VTI) media. The exact travel times are implemented for C-wave Kirchhoff prestack time migration:

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$$t = t_{\mathbf{P}} + t_{\mathbf{S}} \,. \tag{27}$$

For v(z) vertical transverse isotropy (VTI) media, we have the following equations:

$$t_{\rm P} = \sum_{i=1}^{n} \frac{\Delta t_{\rm P0i} \, \nu_{\rm P0i} / \nu_{\rm Pi} (p_{\rm P}, \nu_{\rm P0i}, \nu_{\rm S0i}, \varepsilon_i, \delta_i)}{\sqrt{1 - p_{\rm P}^2 \nu_{\rm Pi}^2 (p_{\rm P}, \nu_{\rm P0i}, \nu_{\rm S0i}, \varepsilon_i, \delta_i)}}, \tag{28}$$

$$t_{S} = \sum_{i=1}^{n} \frac{\Delta t_{S0i} \, v_{S0i} / v_{Si} (p_{S}, v_{P0i}, v_{S0i}, \varepsilon_{i}, \delta_{i})}{\sqrt{1 - p_{S}^{2} v_{Si}^{2} (p_{S}, v_{P0i}, v_{S0i}, \varepsilon_{i}, \delta_{i})}},$$
(29)

$$h_{\rm P} = \sum_{i=1}^{n} \frac{p_{\rm P} v_{\rm Pi}(p_{\rm P}, v_{\rm P0i}, v_{\rm S0i}, \varepsilon_i, \delta_i) v_{\rm P0i} \Delta t_{\rm P0i}}{\sqrt{1 - p_{\rm P}^2 v_{\rm Pi}^2(p_{\rm P}, v_{\rm P0i}, v_{\rm S0i}, \varepsilon_i, \delta_i)}},$$
(30)

$$h_{S} = \sum_{i=1}^{n} \frac{p_{S} v_{Si}(p_{S}, v_{P0i}, v_{S0i}, \varepsilon_{i}, \delta_{i}) v_{S0i} \Delta t_{S0i}}{\sqrt{1 - p_{S}^{2} v_{Si}^{2}(p_{S}, v_{P0i}, v_{S0i}, \varepsilon_{i}, \delta_{i})}},$$
(31)

where  $h_P$  and  $h_S$  are the horizontal distance from the source / receiver to the scatter point,  $p_P$  and  $p_S$  are the P- and S-wave ray parameters,  $\Delta t_{P0i}$  and  $\Delta t_{S0i}$  are the vertical-traveltimes in the *i*-th layer,  $v_{P0i}$  and  $v_{S0i}$  are the vertical velocities of the i-th layer, and  $v_{Pi}$  and  $v_{Si}$  are the group velocities. In a further embodiment, based on the work of Thomsen (1986), we derive the group velocities as a function of  $p_P$  /  $p_S$ ,  $v_{P0i}$ ,  $v_{S0i}$ ,  $\varepsilon_i$  and  $\delta_i$  numerically. The ray parameters in equations (28)-(29) are not time-variant, and  $h_P$  and  $h_S$  are constant for a given scatter point, so we numerically solve equations (30) and (31) for  $p_P$  and  $p_S$ . To compute travel times  $t_P$  and  $t_S$ , we still need to know  $\Delta t_{P0i}$ ,  $\Delta t_{S0i}$ ,  $v_{P0i}$ ,  $v_{S0i}$ ,  $\varepsilon_i$  and  $\delta_i$ . Parameters  $\Delta t_{S0i}$  and  $v_{S0i}$  are not be measured or estimated directly from P-wave and C-wave data. In a further embodiment, we replace them by the C-wave vertical-travel-time

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$$\Delta t_{\text{C0}i} = \Delta t_{\text{P0}i} + \Delta t_{\text{S0}i} \,, \tag{32}$$

and the interval vertical-travel-time ratio, that is the same as the vertical-velocity-ratio for the i-th layer,

$$\gamma_{0i} = \Delta t_{S0i} / \Delta t_{P0i} = v_{P0i} / v_{S0i} . \tag{33}$$

In a further embodiment, with equations (32) and (33),  $\Delta t_{P0i}$  is also replaced by  $\Delta t_{C0i}$  and  $\gamma_{0i}$ . Velocity  $\nu_{P0i}$  is determined from P-wave short-spread moveout velocity  $\nu_{P2i}$ , but the P-wave velocity is indexed at P-wave times and is mapped to C-wave times using  $\gamma_{0i}$ . In a further embodiment, parameter  $\gamma_{0i}$  is determined by correlating corresponding P-wave and C-wave events from stacked sections or near-offsets of prestack gathers and it is unavoidable with errors. P-wave velocity  $\nu_{P2i}$  often has its own error. If the P-wave velocity error is propagated through  $\gamma_{0i}$  to C-wave migration, it is more difficult to take it out without joint processing of both P- and C-wave data. Alternatively, a C-wave velocity is used to control the C-wave migration. In still a further embodiment, using the definition of the C-wave interval velocity of Thomsen (1999),

$$v_{\text{C}i}^2 = \frac{v_{\text{P}2i}^2}{1 + \gamma_{0i}} + \frac{v_{\text{S}2i}^2}{1 + 1/\gamma_{0i}},\tag{34}$$

where

$$v_{P2i}^2 = v_{P0i}^2 (1 + 2\delta_i), \tag{35}$$

$$v_{S2i}^2 = v_{S0i}^2 (1 + 2\sigma_i), \tag{36}$$

$$\sigma_i = \gamma_{0i}^2 (\varepsilon_i - \delta_i), \tag{37}$$

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we replace  $v_{P0i}$  and  $v_{S0i}$  with  $v_{Ci}$ ,  $\gamma_{0i}$ ,  $\varepsilon_{i}$  and  $\delta_{i}$ . Thus, the total diffraction travel time is accurately computed with four parameters  $v_{Ci}$ ,  $\gamma_{0i}$ ,  $\varepsilon_{i}$  and  $\delta_{i}$  at a given C-wave vertical-travel-time  $t_{C0}$ .

In various embodiments, we do not have  $\gamma_{eff}$  (Thomsen, 1999) which requires P-wave velocities. The v(z) effect in travel times is reflected in the interval velocity  $v_{Ci}$  and the interval  $\gamma_{0i}$ . The VTI effect is reflected in anisotropic parameters  $\varepsilon_i$  and  $\delta_i$  directly.

The exact travel time computation does not increase the migration runtime much because for prestack time migration, a small travel timetable is built at each scatter point and it does not change with the input traces.

In an even further embodiment, the following equations are used to compute the pseudo-offset for the C-wave migration of VTI v(z) media

$$t = t_{\rm P}(p_{\rm P}) + t_{\rm S}(p_{\rm S}),$$
 (38)

$$t^*(p) = t, (39)$$

$$t^*(p) = t_P(p) + t_S(p),$$
 (40)

$$x = h_{\rm P}(p) + h_{\rm S}(p),$$
 (41)

Those of ordinary skill in the art will recognize that the pseudo travel time  $t^*$  is no longer hyperbolic. Therefore, velocity analysis based on the pseudo travel time equation becomes complicated.

In an even further embodiment, a method of performing velocity analysis is provided. As illustrated in Figure 5, the method comprises computing (510) a moveout travel time based on an initial model, computing (520) an intermediate travel time,

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mapping (530) a gather from the moveout travel time to the intermediate travel time, and scanning (540) or velocities based on the intermediate travel time.

In even further alternate embodiments, the gather for velocity analysis is a pseudo-offset gather, a migration image gather, a CDP gather, or a CCP gather or any other seismic gather that will occur to those of ordinary skill in the art.

In further alternate embodiments, computing (510) a moveout travel time is based on a simple straight ray, a complicated ray tracing algorithm for VTI v(z) media, or any other travel time algorithm that will occur to those of ordinary skill in the art.

In an even further embodiment, computing (520) an intermediate travel time is based on an equation which has a scannable parameter for the final velocity. In further alternate embodiments, the scannable parameter is a P-wave velocity, an S-wave velocity, a C-wave velocity for converted waves or any other scannable parameter that will occur to those of ordinary skill in the art.

In one example embodiment of the present invention, the method for C-wave velocity analysis of v(z) VTI media comprises computing the moveout travel time based on equation (40) using initial model parameters and computing the intermediate travel time based on following equation:

$$t^{2} = t_{C0}^{2} + \frac{x^{2}}{V_{C2}^{2}} \left(1 - \frac{Ax^{2}}{t_{C0}^{2} + Ax^{2}/1 - 1/\gamma_{0}}\right), \quad A = \frac{(\gamma_{0} - 1)^{2}}{4\gamma_{0}V_{C2}^{2}}, \tag{42}$$

where  $\mathcal{H}$  is the average vertical travel time ratio and  $V_{C2}$  is a scannable velocity parameter. The final C-wave interval velocity  $v_{Ci}$  is determined from  $V_{C2}$  based on the following Dix formula:

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$$v_{Ci}^{2} = \frac{t_{C0i}V_{C2}^{2}(t_{C0i}) - t_{C0i-1}V_{C2}^{2}(t_{C0i-1})}{t_{C0i} - t_{C0i-1}} . \tag{43}$$

In various example embodiments discussed above, travel times, pseudo travel times, moveout travel times, projected travel times, have been computed using various algorithms. It will occur to those of ordinary skill in the art that travel times used in the present invention may be determined using any of the various travel time algorithms that will occur to those of ordinary skill in the art.

In a further embodiment, a system is provided for migrating an input seismic data point having an input source location and an input receiver location, a scatter point, and an image location associated therewith. The system comprises means for determining a pseudo-offset. In alternate embodiments, means for determining a pseudo-offset comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art. The method further comprises means for mapping the seismic data point to the image location based at least in part on the pseudo-offset. In alternate embodiments, means for mapping comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In an even further embodiment, the system further comprises means for determining a pseudo-source and a pseudo-receiver. In alternate embodiments, means for determining a pseudo-source and a pseudo-receiver comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

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In an even further embodiment, the system further comprises means for determining a pseudo ray parameter. In alternate embodiments, means for determining a pseudo ray parameter comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In still a further embodiment, said means for determining a pseudo ray parameter further comprises means for determining a pseudo ray parameter dependant at least in part upon the ray parameter down from the input source location to the scatter point and the ray parameter up from the scatter point to the input receiver location. In alternate embodiments, means for determining a pseudo ray parameter comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In yet a further embodiment, said means for determining a pseudo-offset further comprises means for determining an input travel time associated with the input source location, the input receiver location, and the scatter point. In alternate embodiments, means for determining an input travel time comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In a further embodiment, means for determining a pseudo-offset further comprises means for determining a pseudo travel time from the pseudo-source to the pseudo-receiver via the scatter point. In alternate embodiments, means for determining a pseudo travel time comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

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In a further embodiment, the system further comprises a means for migration stacking. In alternate embodiments, means for migration stacking comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In a further embodiment, said means for migration stacking further comprises means for determining a moveout travel time. In alternate embodiments, means for determining a moveout travel time comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In still a further embodiment, the system further comprises means for summing the data point along the moveout travel time. In alternate embodiments, means for summing comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In a further embodiment a system is provided for migration of a seismic data point having an input source location, an input receiver location, and a scatter point associated therewith. The system comprises means for determining a projected source location. In alternate embodiments, means for determining a projected source location comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art. The system further comprises means for determining a projected receiver location. In alternate embodiments, means for determining a projected receiver location comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of

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ordinary skill in the art. The system further comprises means for mapping the seismic data point from an input travel time to a projected travel time. In alternate embodiments, means for mapping comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art. The system further comprises means for determining a pseudo-offset based on the projected travel time. In alternate embodiments, means for determining a pseudo-offset comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art. The system further comprises means for mapping the data point to the pseudo-offset. In alternate embodiments, means for mapping comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In an even further embodiment, the system further comprises means for determining a raypath from said input source location to said input receiver location. In alternate embodiments, means for determining a raypath comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In still a further embodiment, said means for determining a projected receiver location further comprises means for determining a projected receiver location along the determined raypath. In alternate embodiments, means for determining a projected receiver location along the determined raypath comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

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In a further embodiment, said means for determining a projected source location further comprises means for determining a projected source location along the determined raypath. In alternate embodiments, means for determining a projected source location along the determined raypath comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In yet a further embodiment, the system further comprises means for determining a pseudo-source and a pseudo-receiver. In alternate embodiments, means for determining a pseudo-source and a pseudo-receiver comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In still a further embodiment, the system further comprises means for determining a pseudo ray parameter. In alternate embodiments, means for determining a pseudo ray parameter comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In an even further embodiment, said means for determining a pseudo-offset further comprises means for determining a projected travel time associated with the projected source location, the projected receiver location, and the scatter point. In alternate embodiments, means for determining a projected travel time comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

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In an even further embodiment, means for determining a pseudo-offset further comprises means for determining a pseudo travel time from a pseudo-source to a pseudo-receiver via the scatter point. In alternate embodiments, means for determining a pseudo travel time from a pseudo-source to a pseudo-receiver via the scatter point comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In an even further embodiment, the system further comprises means for migration stacking. In alternate embodiments, means for migration stacking comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In an even further embodiment, said means for migration stacking further comprises means for determining a moveout travel time. In alternate embodiments, means for determining a moveout travel time comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In yet a further embodiment, the system further comprises means for summing the data point along the moveout travel time. In alternate embodiments, means for summing comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

In still a further embodiment, a system for performing velocity analysis on a seismic gather is provided. The system comprises means for computing a moveout travel time based on an initial model. In alternate embodiments, means for computing a

moveout travel time based on an initial model comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art. The system further comprises means for computing an intermediate travel time. In alternate embodiments, means for computing an intermediate travel time comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art. The system further comprises means for mapping the gather from the moveout travel time to the intermediate travel time. In alternate embodiments, means for mapping comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art. The system further comprises means for scanning for velocities based on the intermediate travel time. In alternate embodiments, means for scanning comprise a computer, a workstation, or software running on any computer, or any other means that will occur to those of ordinary skill in the art.

The example method embodiments are described for the purpose of teaching the broad aspect of the invention only. Systems, apparatuses, and the seismic product of the methods are also described and claimed as the present invention. For further example embodiments of the present invention, readers are directed to exhibits A and B attached, incorporated, and made a part of this patent application in compliance with 37 CFR 1.91. Exhibit A is an unpublished abstract describing further example embodiments of the present invention. Exhibit B is also an unpublished abstract describing further example embodiments of the present invention.